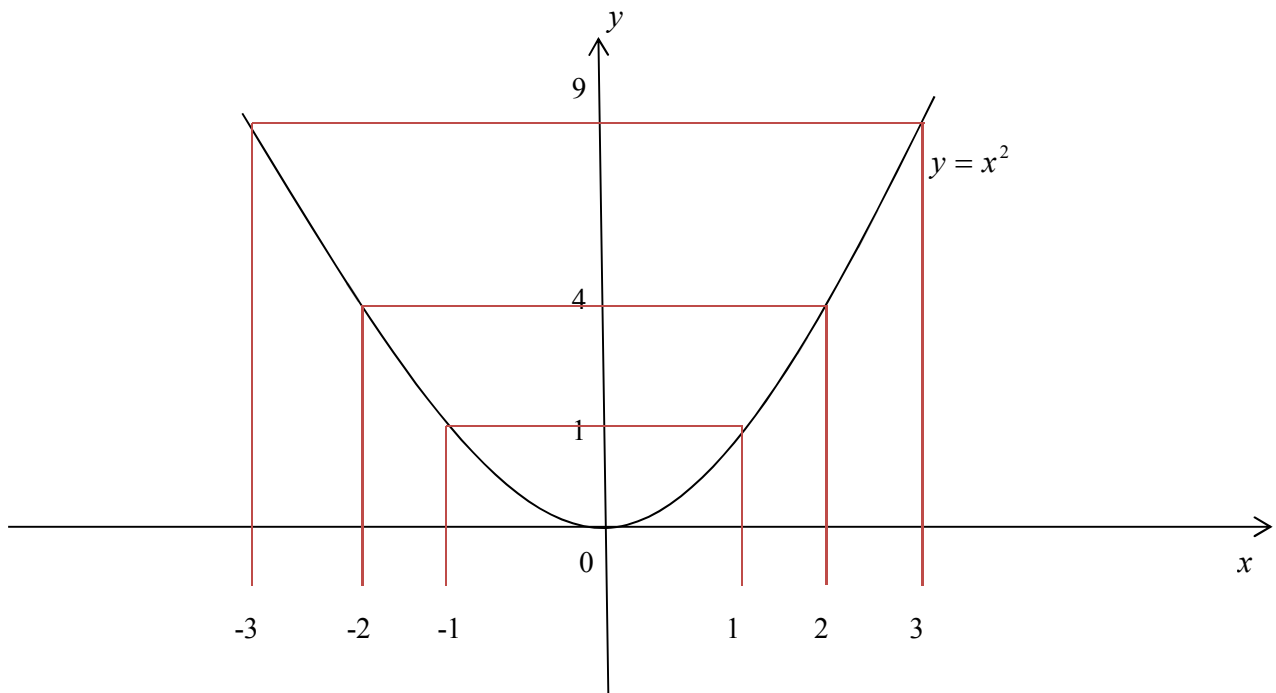


Why is the basic parabola  $y = x^2$  is symmetrical about the  $y$  – axis? Spend a moment to study its graphical output below:



Symmetry exists NOT because the graph looks as such, but because we know that  $(-1)^2 = (1)^2 = 1$  for  $x = \pm 1$ ,  $(-2)^2 = (2)^2 = 4$  for  $x = \pm 2$ ,  $(-3)^2 = (3)^2 = 9$  for  $x = \pm 3$ . And we can clearly see that things don't just end there, because to prove it is also true for all  $x \in \mathfrak{R}$ , a non-exhaustive list of attempts must be undertaken.

Which is why we seek to apply a general treatment of the above observation, and it can be stated as follows:

For  $y = f(x)$ , its graph is **symmetrical** about the  $y$  – axis for all  $x \in (-a, a)$  where  $a$  is a positive real value **IF AND ONLY IF**  $f(x) = f(-x)$ .

Applying this assertion to  $y = x^2$ , we have  $(x)^2 = (-x)^2$ ; so yes we can conclude the parabola is indeed a reflection of itself in the vertical axis.